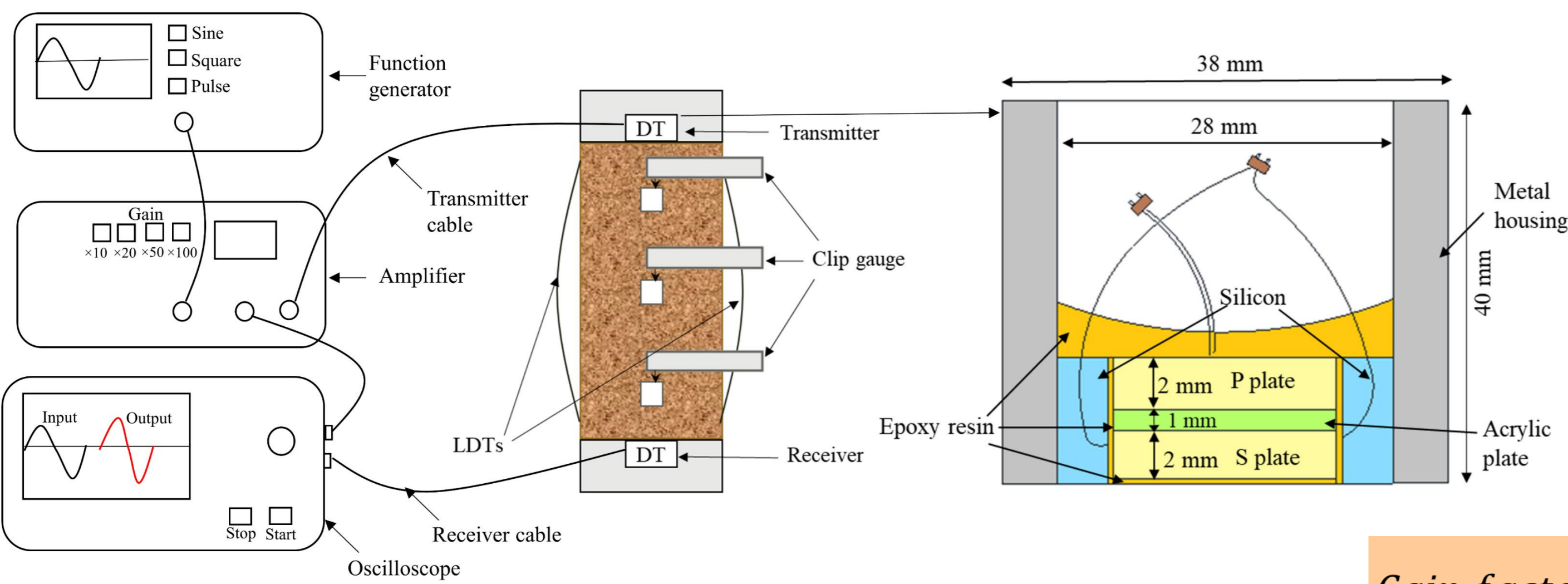
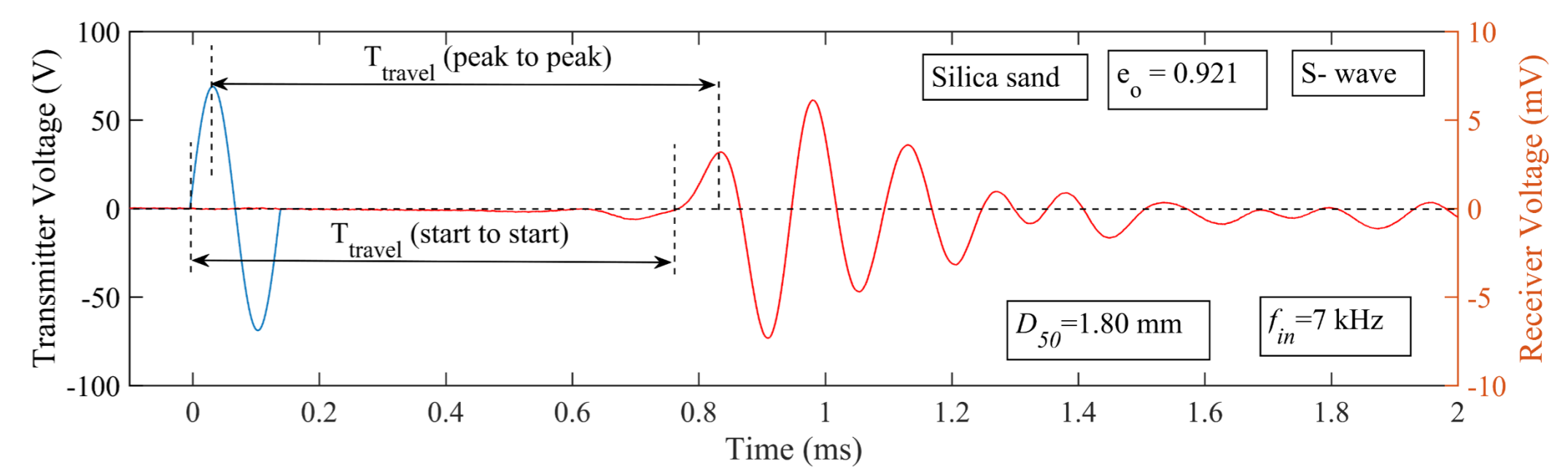


For assemblies of spherical particles with Hertzian contacts, the stress wave velocities should not depend on median particles size ( $D_{50}$ ). However, a link between  $D_{50}$  and stress wave velocity has been reported in experiments. To identify the reasons for discrepancies, wave velocity measurements were performed using disk transducers on four different  $D_{50}$  glass beads. The results indicate that shear ( $V_s$ ) and compression ( $V_p$ ) wave velocities are independent of  $D_{50}$ . The maximum frequency that can propagate through a granular assembly (lowpass frequency) reduces with increasing  $D_{50}$ . For  $V_s$ , selected input frequencies should match frequencies which exhibit largest gain factors and input frequencies should not exceed half of lowpass frequency. To determine  $V_p$ , it is suggested to adopt start to start method and to choose an input frequency which is slightly lower than the lowpass frequency.

### Assembly for stress wave measurements



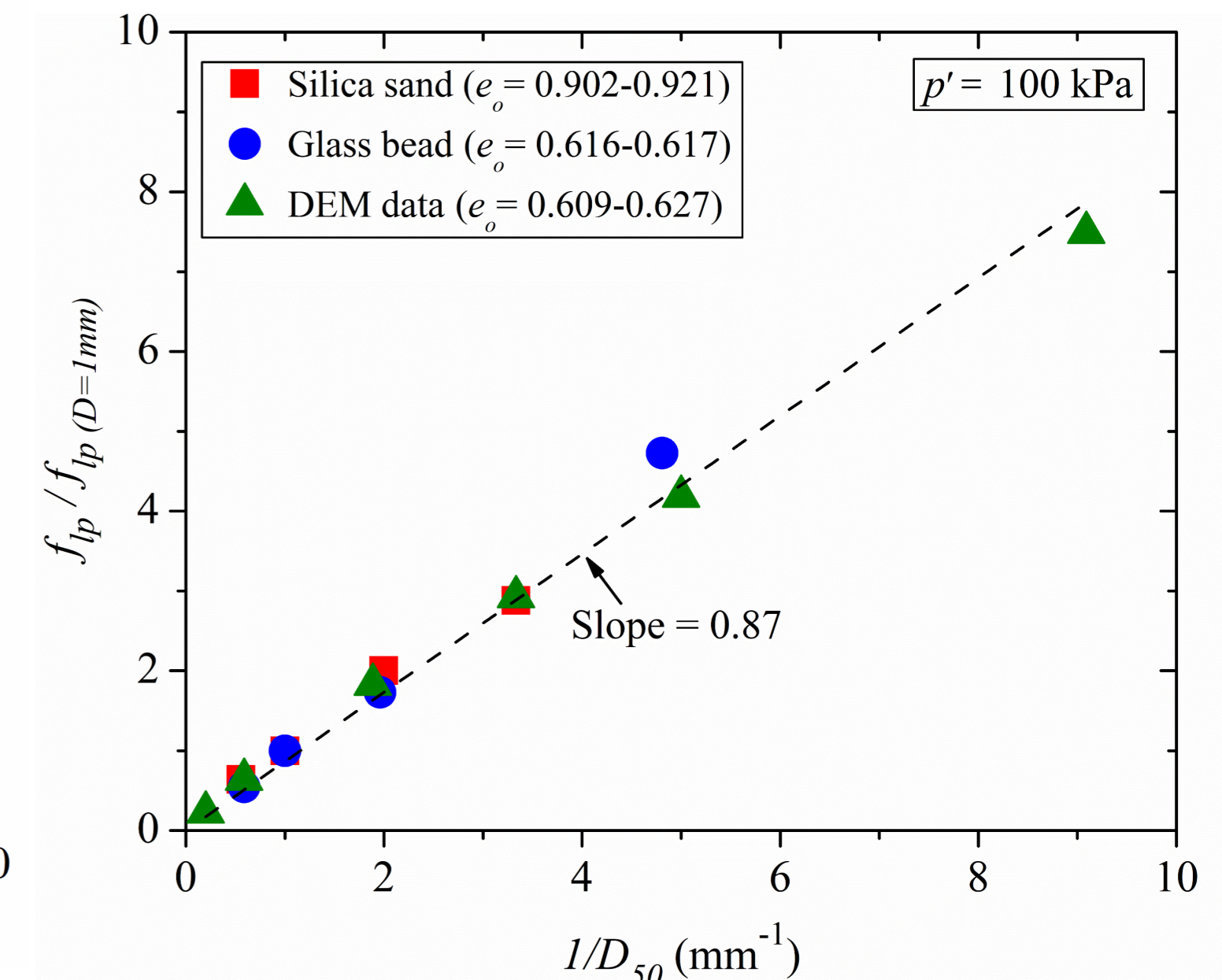
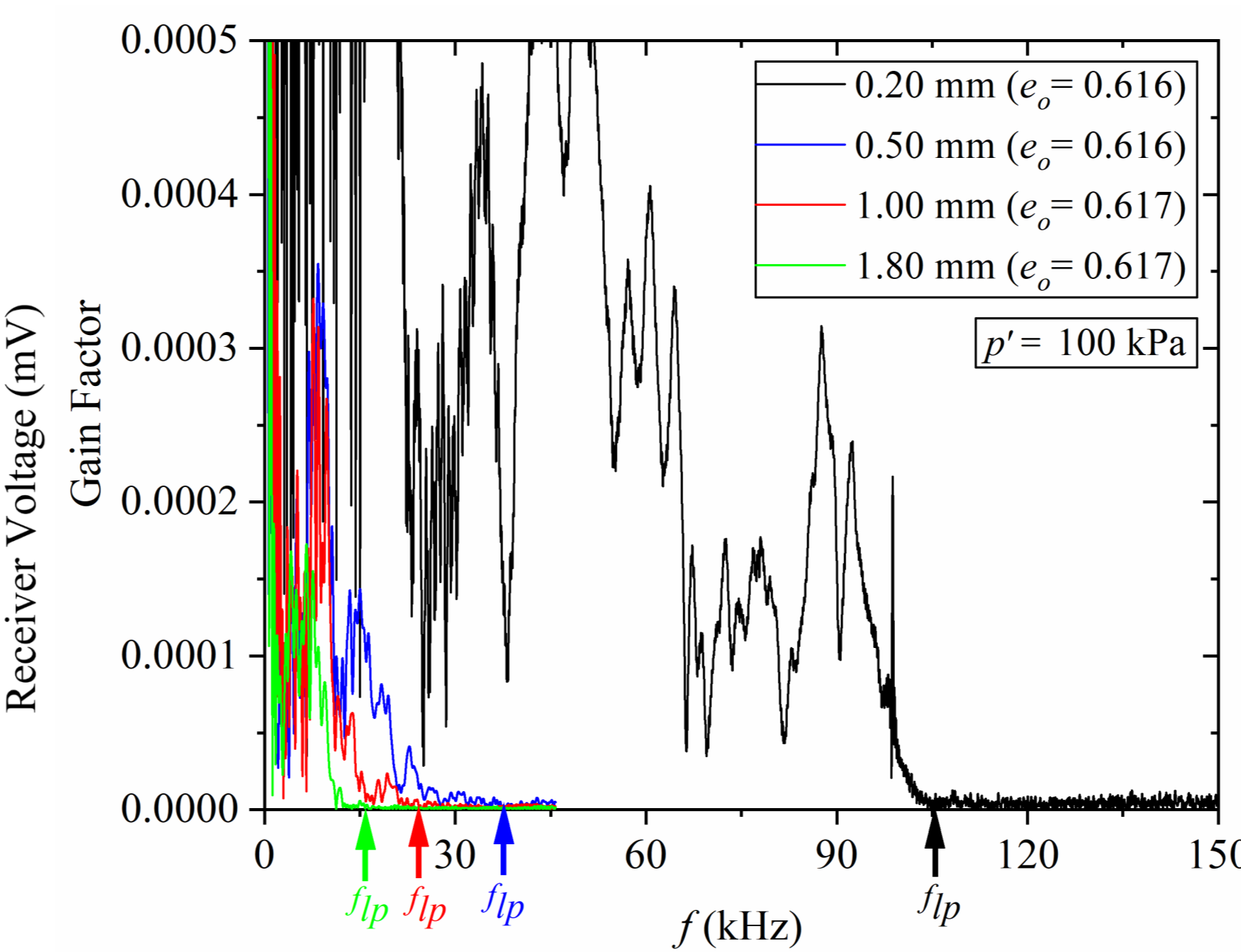
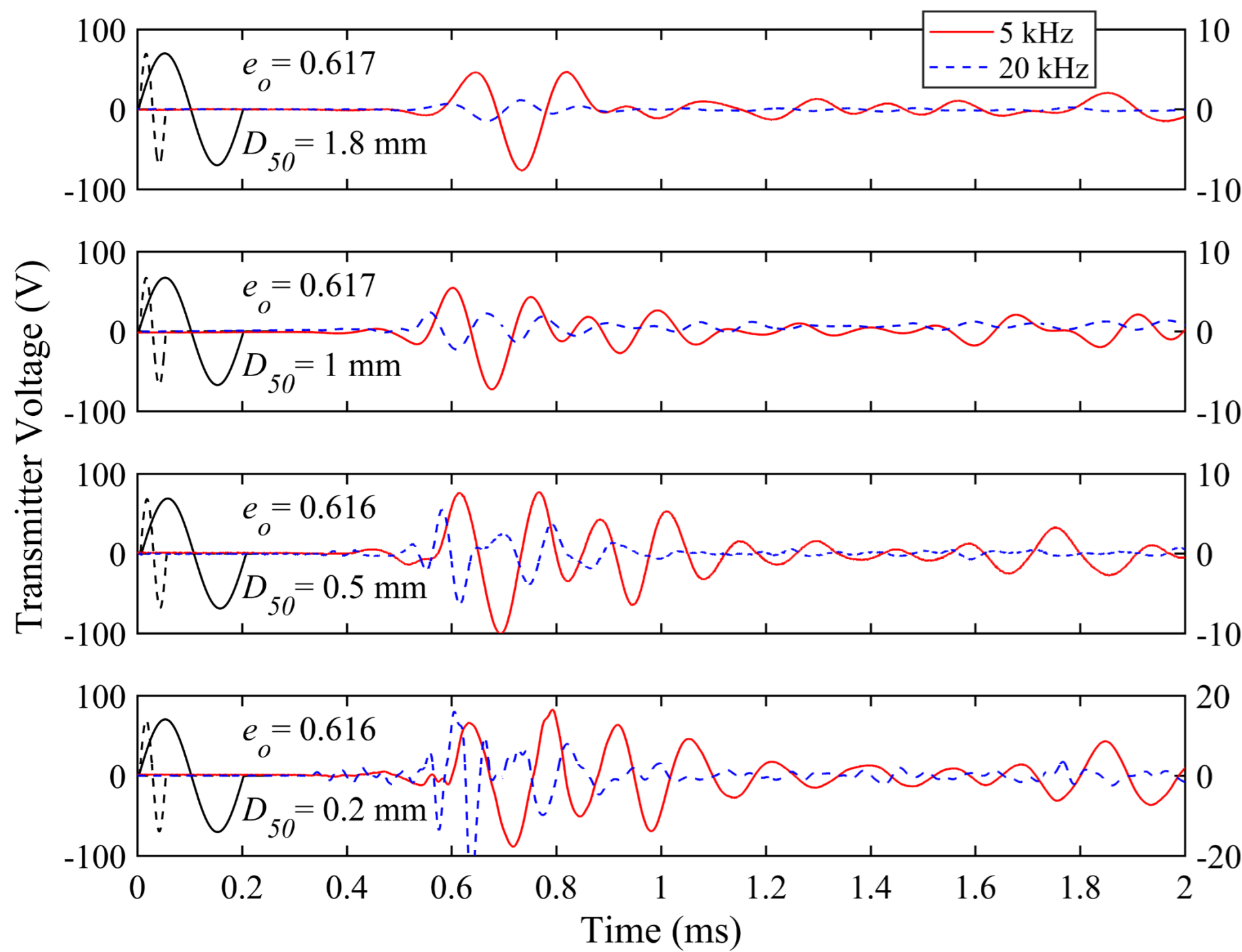
### Two conventional methods for estimating travel time



$$V_s \propto L f_{lp} \quad (\text{from dispersion theory})$$

$$\text{Gain factor} = \frac{FFT_{\text{output}}}{FFT_{\text{input}}}$$

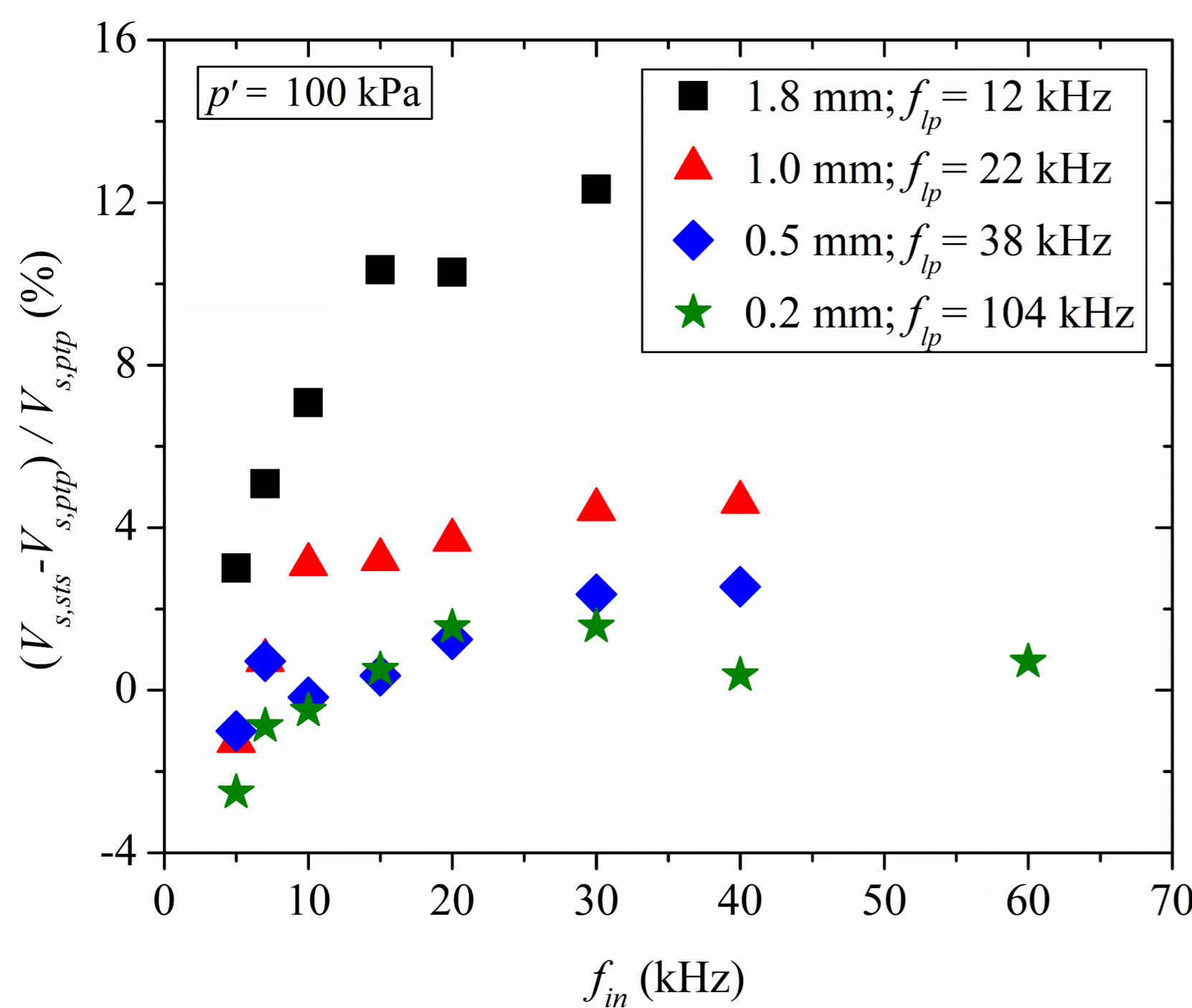
★ Low pass frequency ( $f_{lp}$ ) is the maximum transmitted frequency



★ Range of frequency propagation increases with decreasing  $D_{50}$

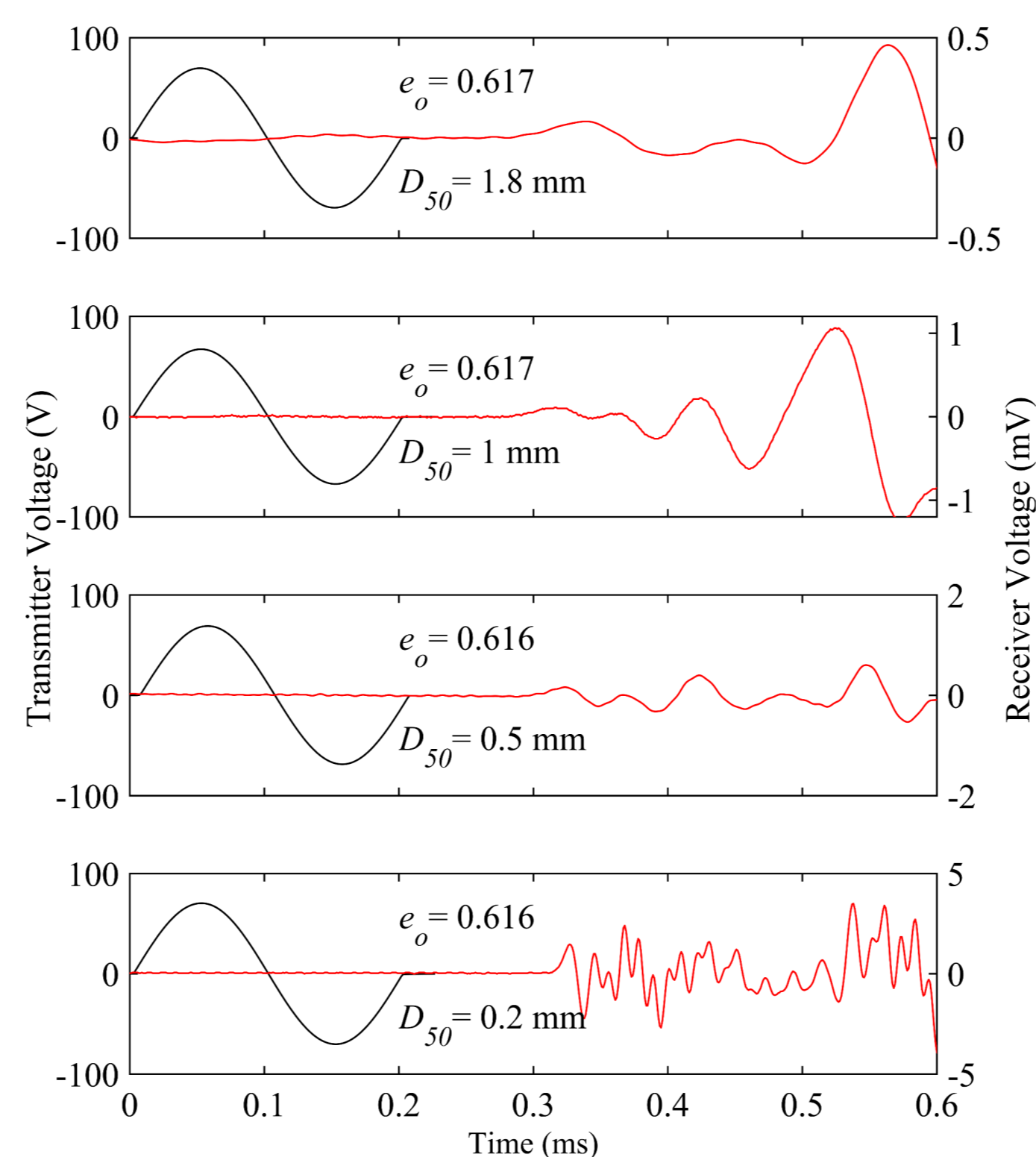
★ Low pass frequency varies linearly with  $1/D_{50}$

★ S-wave travel time is independent of  $D_{50}$



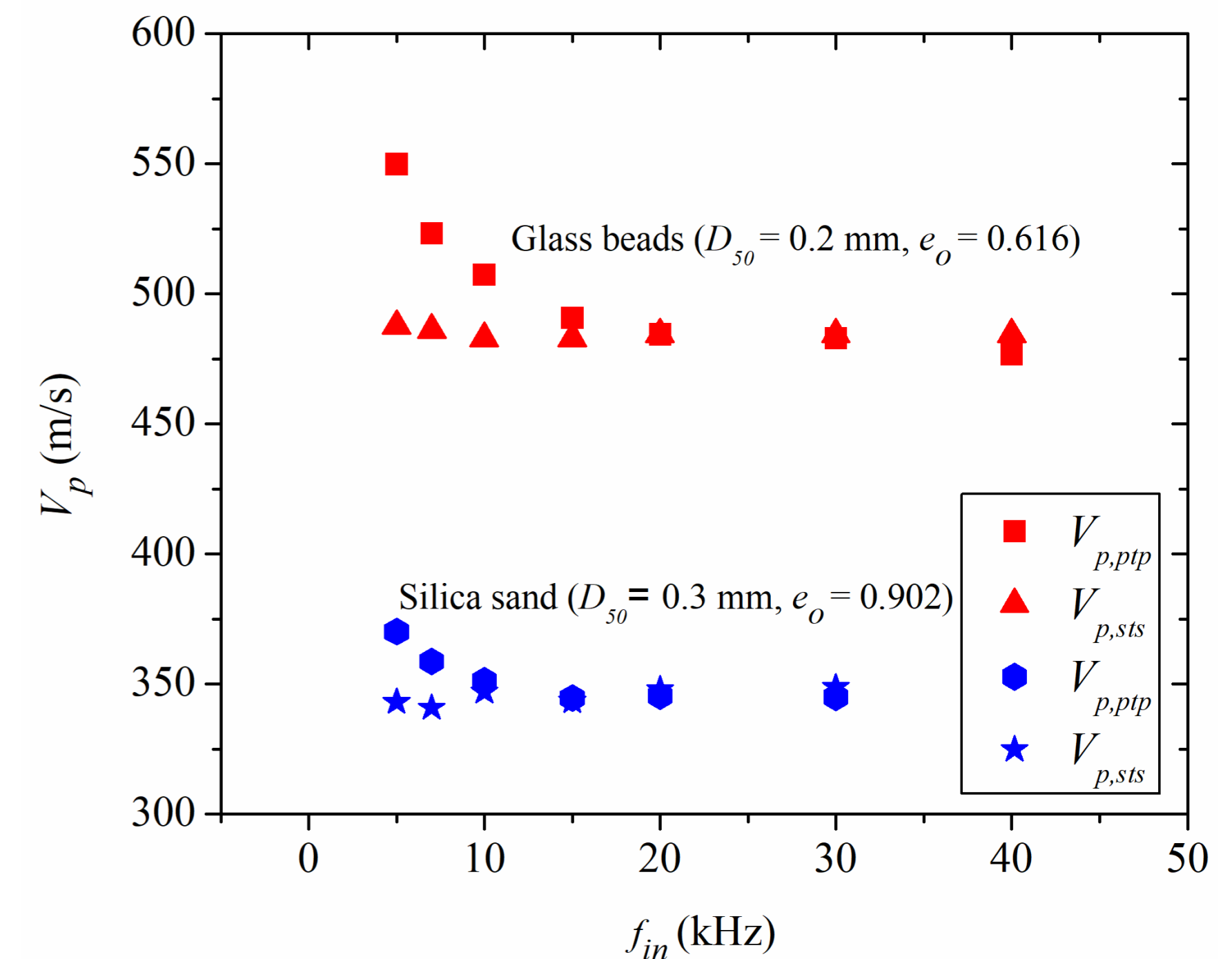
★ % difference between  $V_s$  measured from sts and ptp increases, when  $f_{in} < f_{lp}/2$

★ For  $V_s$ ,  $f_{in}$  should match frequencies which have maximum gain factors and  $f_{in}$  should not exceed  $f_{lp}/2$



★ P-wave travel time is independent of  $D_{50}$

★ Wave lengths of output signal does not match input for lower  $D_{50}$  specimens



★ Peak to peak method overestimates the P-wave velocities

★ For  $V_p$ , start to start method and  $f_{in} < f_{lp}$  should be used

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